

M. Sc.  
MATHEMATICS  
ALGEBRA

M.Sc.-M (P)-C1

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M.Sc. MATHEMATICS - 1<sup>st</sup> Year

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M.Sc.-M (P)-C5

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**M.Sc.(F)-M-C8A**

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